# DSC 190 DATA STRUCTURES & ALGORITHMS

Lecture 15 | Part 1

**Today's Lecture** 

## **String Data Structures**

- One of the themes of this quarter:
- If you're doing something once, use an algorithm.
- If you're doing it over and over, use an appropriate data structure.

# **String Data Structures**

- Over the next two lectures, we'll look at data structures for strings.
- Today: tries for efficient repeated prefix queries.

# **Autocompletion**



# DSC 190 DATA STRUCTURES & ALGORITHMS

Lecture 15 | Part 2

**Tries** 

### Trie

- A data structure for storing strings.
- Pronounced "try", short for "retrieval".
- Supports fast prefix query and membership query.

#### **Prefixes**

► A prefix p of a string s is a contiguous slice of the form s[o:t], for some t.

#### Examples:

- "test" is a prefix of "testing"
- "te" is a prefix of "testing"
- "sa" is a prefix of "san diego"
- "di" is not a prefix of "san diego"

# **Prefix Query**

- **Given**: a collection of *n* strings and a prefix, p.
- Find: all strings in the collection for which p is a prefix.

```
Example:
"bar" "bad", "bid", "car"

p = "ba"
```

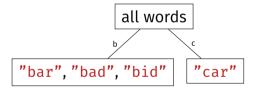
#### **Brute Force**

Loop over each of *n* strings, compare against prefix p.

▶ Worst-case time:  $\Theta(n \cdot |p|)$ 

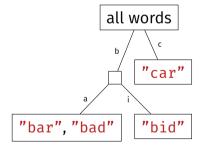
### **Trie: Motivation**

"bar", "bad", "bid", "car"



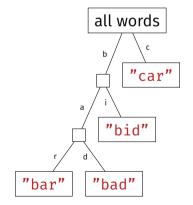
### **Trie: Motivation**

"bar", "bad", "bid", "car"



# **Trie: Motivation**

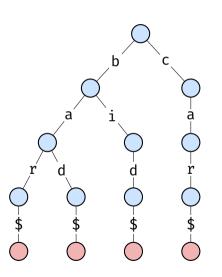
"bar", "bad", "bid", "car"



### **Tries**

- Internal nodes represent prefixes.
- Leaf nodes represent full words.
- Edges are characters.
- Words are encoded as paths.

### **Sentinels**



- ▶ \$ is a **sentinel**.
- It is different from the dollar sign character.
- It marks the end of a word.
- Used to show that "bar" in trie, but "ba" not.

# DSC 190 DATA STRUCTURES & ALGORITHMS

Lecture 15 | Part 3

**Implementing Tries** 

# S="\$" Representation

► Each node has a hash table / array mapping characters to a child nodes.

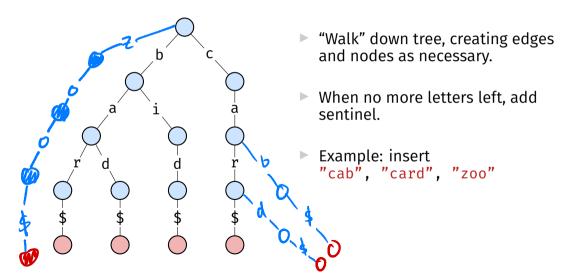
Sentinel represented with a singleton object?

```
END_OF_STRING = object()

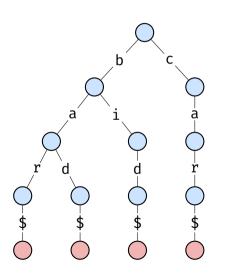
class TrieNode:

    def __init__(self):
        self.children = {}
```

### **Insertion**



# **Insertion (Recursive)**



- Suppose we .insert(s) on root node.
- ► If s[o] not in self.children, create a new node.
- Otherwise, let child be self.children[s[o]].
- Recursively insert s[1:] into child.

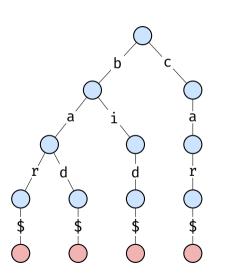
```
def insert(self, s, start=0, stop=None):
    """Insert s[start:stop] into the trie."""
    if stop is None:
        stop = len(s)
    if start >= stop:
        self.children[END OF STRING] = TrieNode()
        return
    if s[start] not in self.children:
        self.children[s[start]] = TrieNode()
```

child = self.children[s[start]]
child.insert(s, start + 1, stop)

# **Insertion Time Complexity**

- $\triangleright$   $\Theta(|w|)$  time, where w is the string inserted.
- No matter how many elements in trie!

#### Walk



- Useful operation.
- Given a prefix, "walk" down tree.
- ► If we "fall off", raise error.
- Otherwise, return last node seen.
- Examples: "ba", "bo"

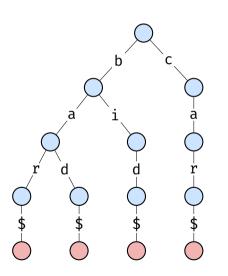
```
def walk(self, s, start=0, stop=None):
    """Walk the trie following s[start:stop].
    Raises ValueError if falls off tree.
    Returns last node encountered otherwise."""
    if stop is None:
        stop = len(s)
    if start >= stop:
        return self
    if s[start] not in self.children:
        raise ValueError('Fell off tree.')
    else:
        child = self.children[s[start]]
        return child.walk(s. start + 1. stop)
```

# **Walk Time Complexity**

Worst-case  $\Theta(|p|)$  time, where p is the prefix searched.

No matter how many elements in trie!

# **Membership Query**



- Given p, return True/False if p in collection.
- "Walk" down tree.
- If we "fall off", return False.
- If not, check that sentinel in children.
- Examples: "ba", "bad"

```
def membership_query(self, s, start=0, stop=None):
    """Determine if s[start:stop] is in trie."""
    try:
        node = self.walk(s, start, stop)
```

return END OF STRING in node.children

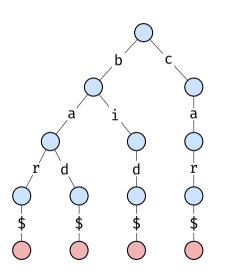
except ValueError: return False

# **Membership Query Time Complexity**

Worst-case  $\Theta(|w|)$  time, where w is the prefix searched.

No matter how many elements in trie!

### **Produce**



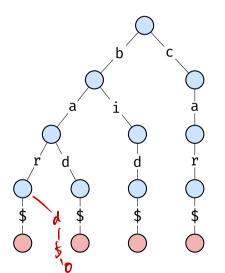
- Goal: generate all words in subtrie.
- Perform a DFS, keeping track of letters along path.
- If we find a sentinel, print path.

```
def produce(self, pathchars=''):
         """Generate the words in the trie."""
         for letter. child in self.children.items():
             if letter is END OF STRING:
                 vield pathchars
             else:
                 yield from child.produce(pathchars + letter)
def even-numbers (): for x in even-numbers (): print (x)
```

# **Produce Time Complexity**

- Worst-case  $\Theta(\ell)$  time, where  $\ell$  is total length of all strings stored in the trie.
- If length strings is considered a constant, this is  $\Theta(n)$ .

# **Prefix Query (Complete)**



- Given p, return all completions.
- "Walk" down tree.
- If we "fall off", return empty list..
- If not, produce all nodes in subtrie.
- Examples: "ba", "bad"

```
Sum (x *x 2 for x in rame())
def complete(self, prefix):
    trv:
        node = self.walk(prefix)
    except ValueError:
        return []
    return list(node.produce())
```

list (prefix + s for s in node. produce())

# **Prefix Query Time Complexity**

- ► Worst-case  $Θ(|p| + ℓ_p)$  time, where p is the prefix searched and  $ℓ_p$  is the total length of all matches.
- If length is considered constant, this is  $\Theta(|p| + z)$ , where z is number of matches.

# DSC 190 DATA STRUCTURES & ALGORITHMS

Lecture 15 | Part 4

**Demo**